



Darcy's Law, valid or not in a contaminant-impacted zone?

(Part 1: membrane porous media)

Dr Xiaohui Chen

Lecturer in Geotechnics

Academic Leader of BioSAS consortium (UoL, UoS, UoY)

Joint Leader of Nuclear Group at Civil (UoL)



Contents

1. Introduction

2. Methodology

3. New Matrix

4. Modelling

5. End

Revisit Darcy's Law (1856)

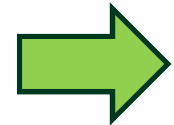
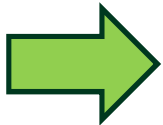


UNIVERSITY OF LEEDS

160 years, forming the basis of hydrogeology, cross-disciplinary used in geotechnics, geochemistry etc.

$$\mathbf{u} = \frac{k}{\nu} \text{grad } p$$

Water



World has changed, and is changing



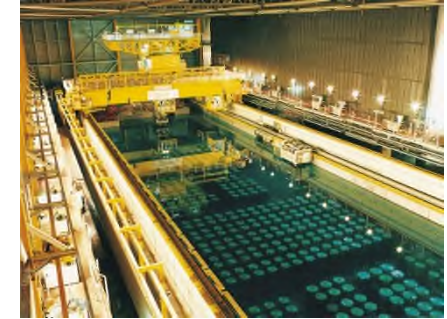
UNIVERSITY OF LEEDS



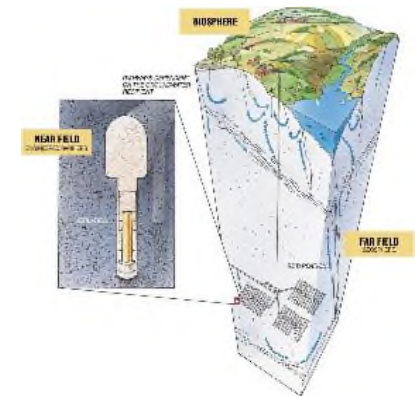
Nuclear: Fukushima (2011)



Landfill example



Waste Geological Disposal

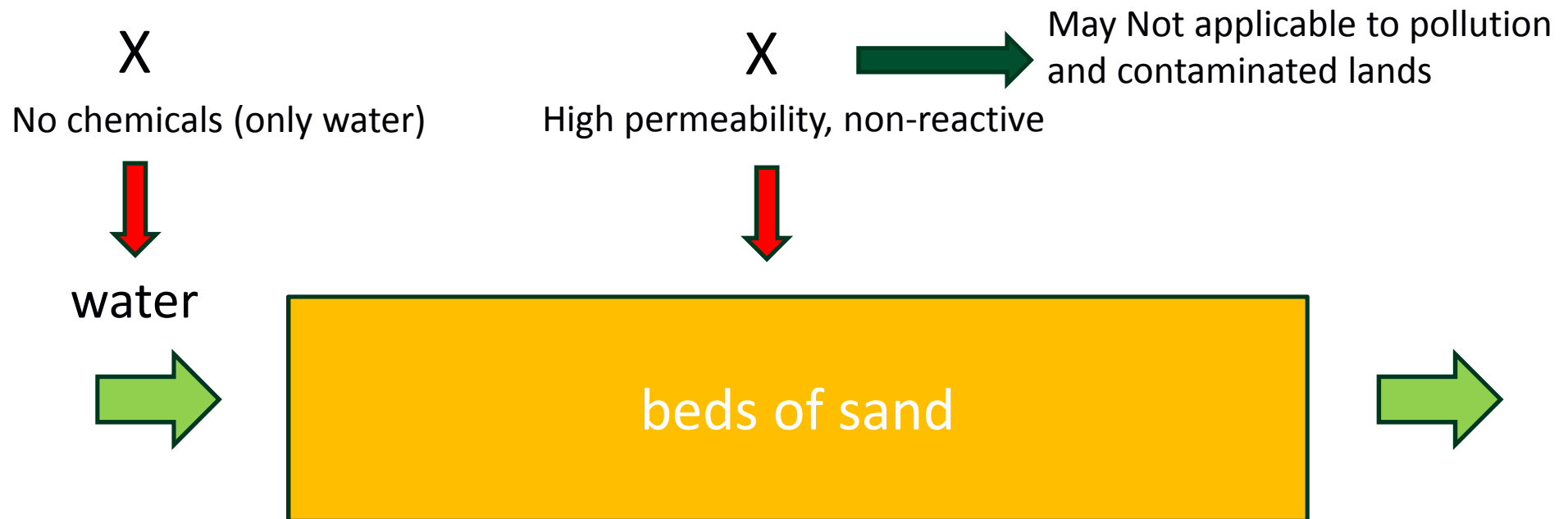


Revisit Darcy's Law (1856)...needs to be changed



UNIVERSITY OF LEEDS

Assumption of Darcy's Law



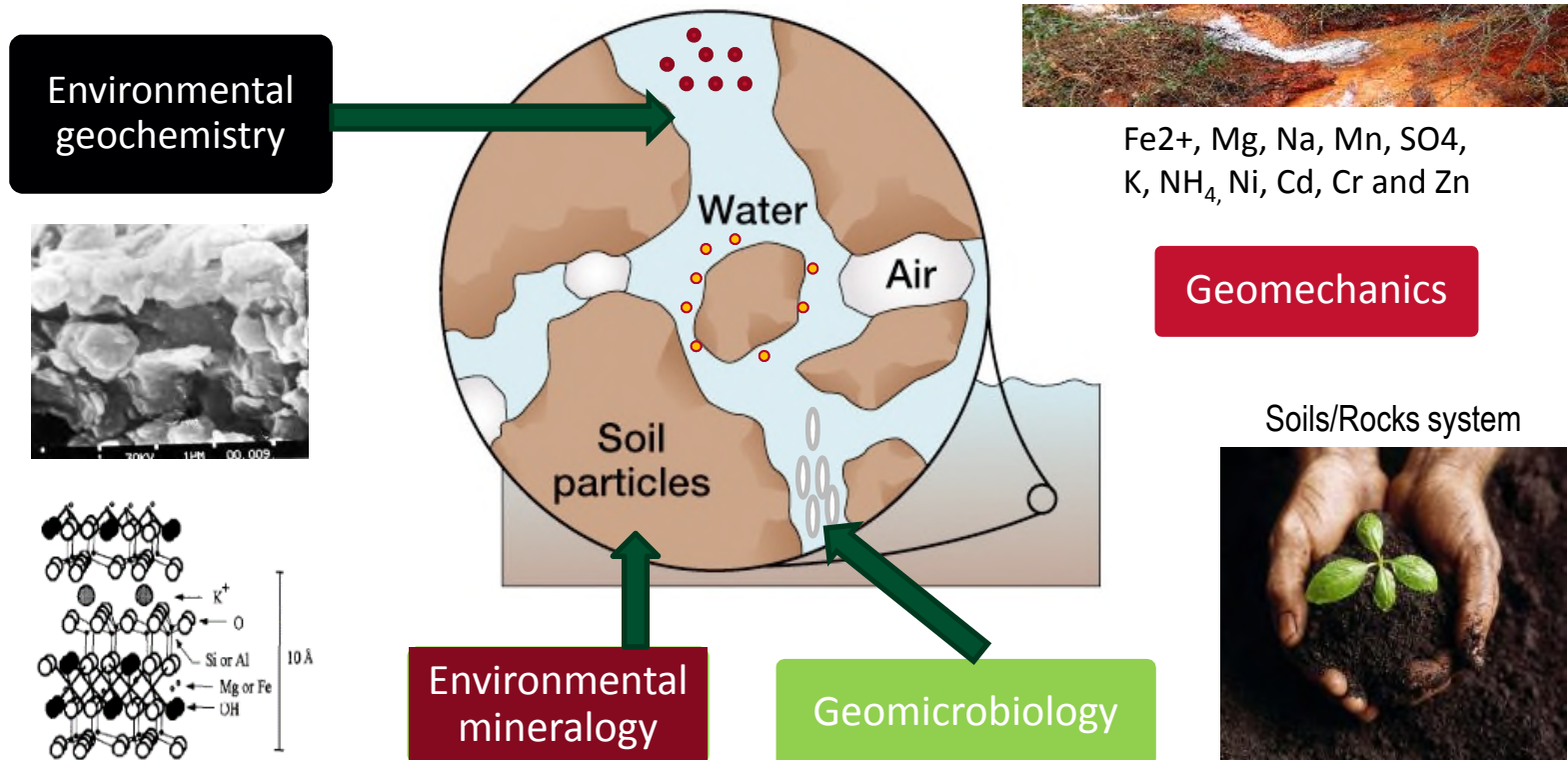
$$\mathbf{u} = \frac{k}{\nu} \text{grad } p$$

Darcy, H. (1856). *Les fontaines publiques de la ville de Dijon*. Paris: Dalmont.

Molecular-scale coupled influence?



UNIVERSITY OF LEEDS

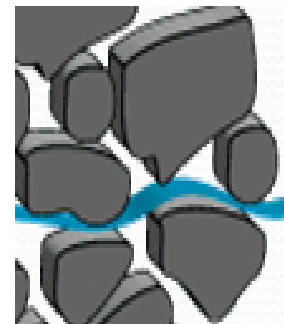
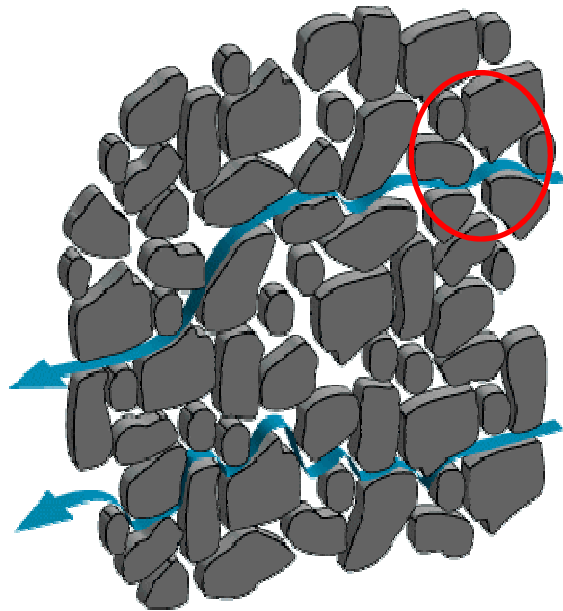


Question: how to incorporate such coupled influence into theoretical prediction?

Conceptual model?



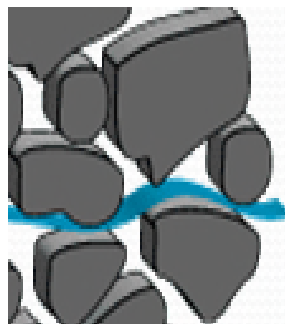
UNIVERSITY OF LEEDS



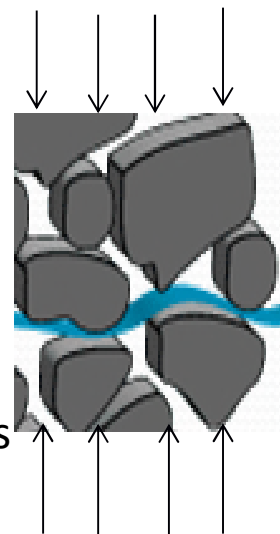
Multiple minerals transfer

Multiple chemicals reaction

Multiple microbes process



Chemical Osmosis
Thermal Osmosis

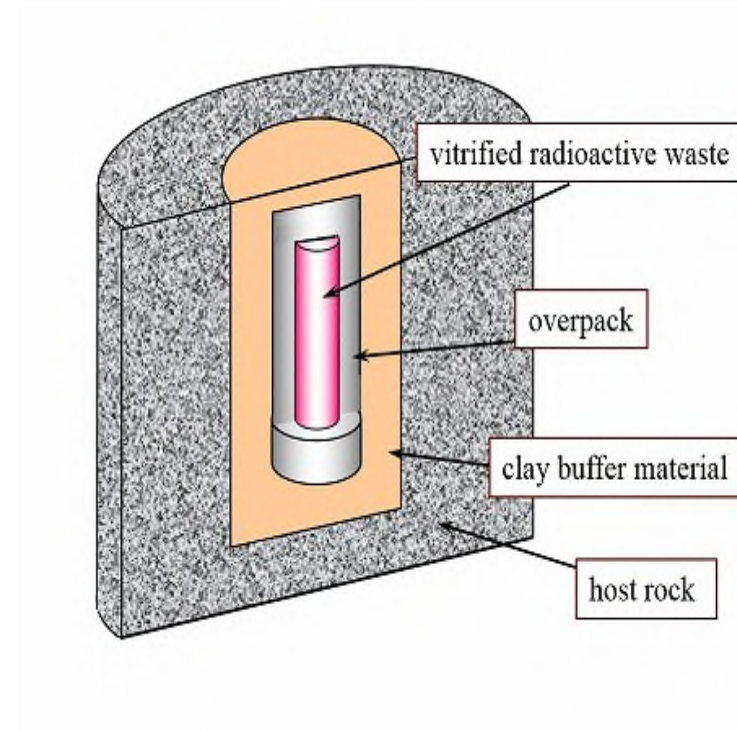
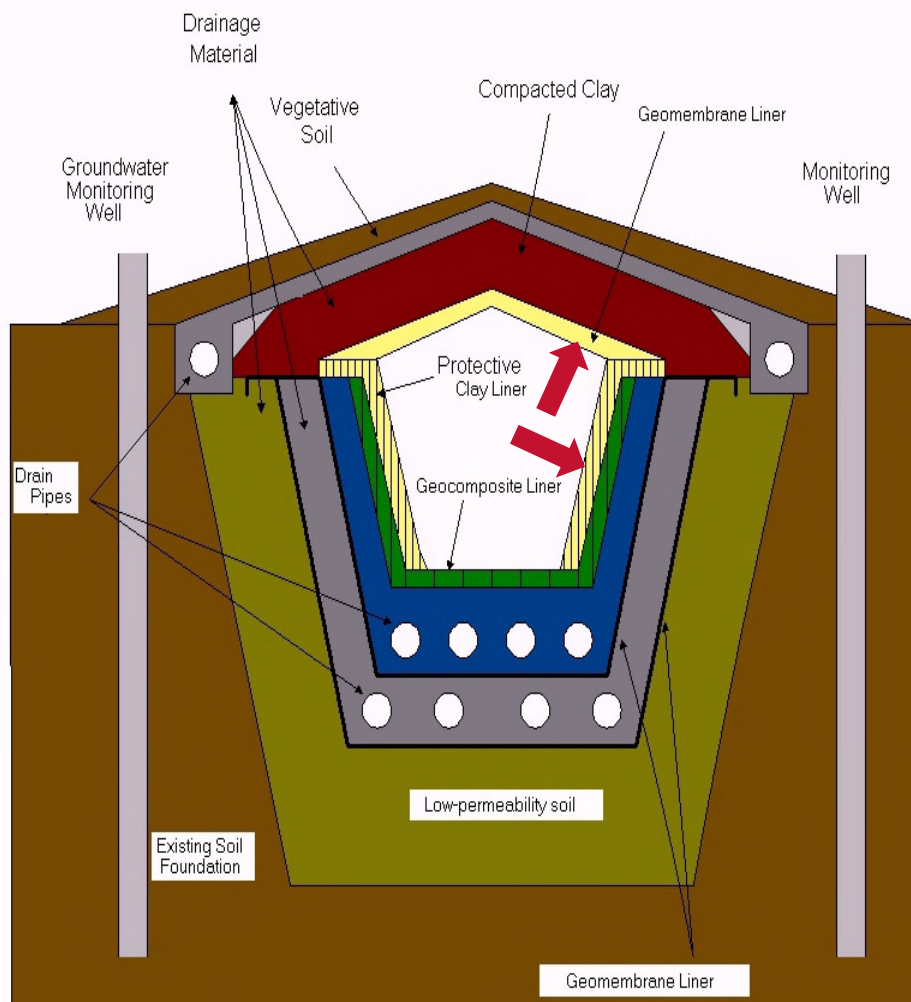


Gas/CO₂/Oil interactions with water

Soil/rock particles deformation



Why low permeability matters?



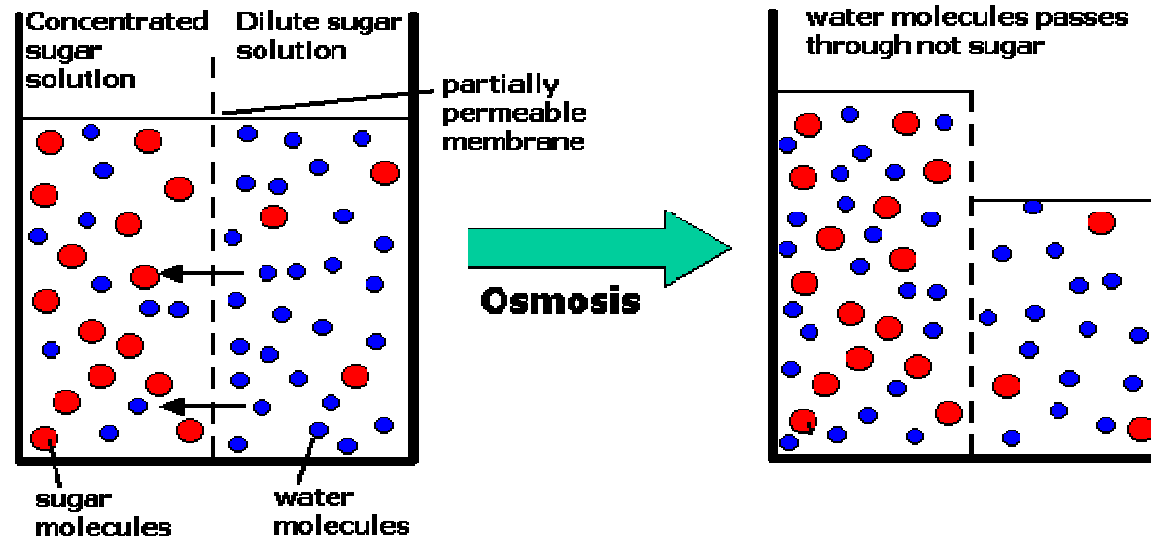
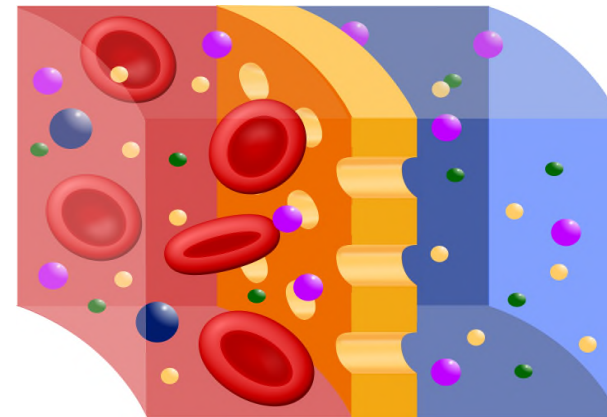
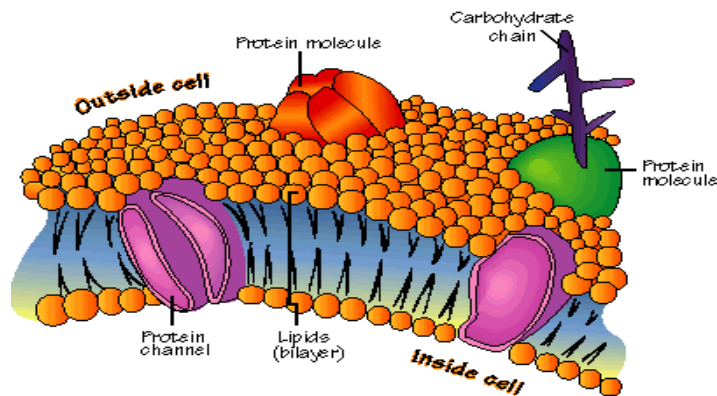
<http://nucl-mater.eng.hokudai.ac.jp/overview-en/theme-en/>

<http://www.keepoklahomabeautiful.com/21st-century-landfills>

Osmosis



UNIVERSITY OF LEEDS





Contents

1. Introduction

2. Methodology

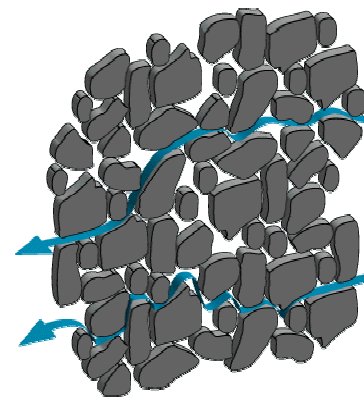
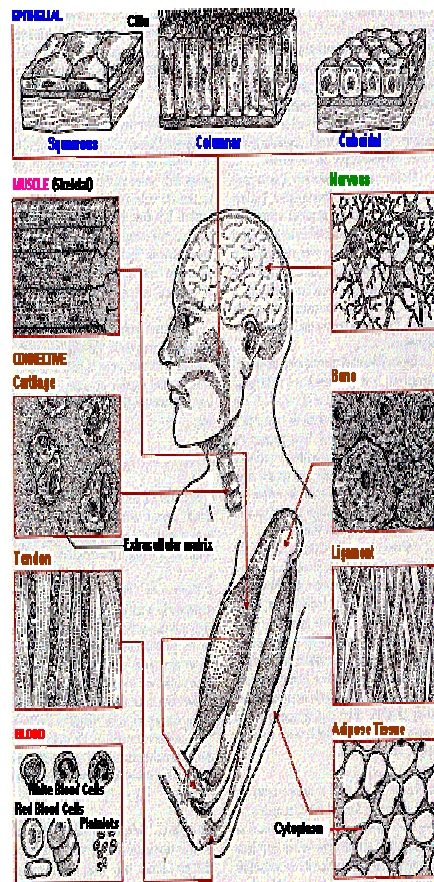
3. New Matrix

4. Modelling

5. End



Mixture Theory



Blood in tissues

≈

groundwater in
soils/rocks

More realistic
More systematic

Mixture Coupling Theory

“a systematic approach..., which can help build coupled formulations based on a *single unified theory*, between geophysics and geochemistry”



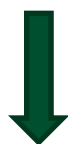
CHEN, X., PAO, W., THORNTON, S. & SMALL, J. 2016. Unsaturated hydro-mechanical–chemical constitutive coupled model based on mixture coupling theory: Hydration swelling and chemical osmosis. *International Journal of Engineering Science* (IF:3.165), 104, 97-109.



Entropy

Second law of thermodynamics

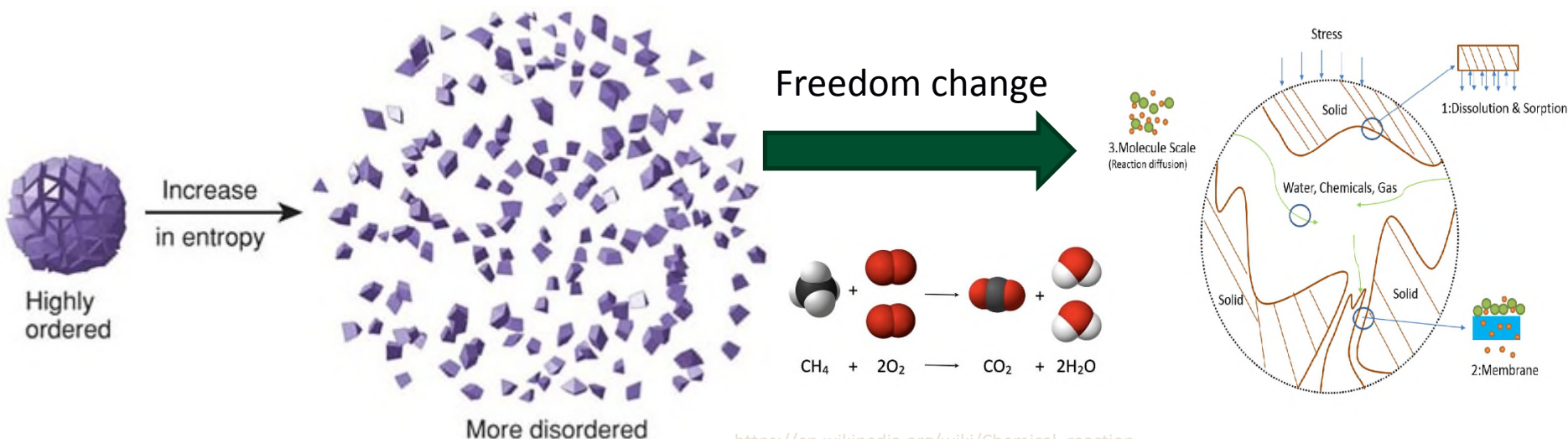
The entropy of an isolated system not in equilibrium will tend to increase over time, approaching a maximum value at equilibrium



Interpreted as the degree of disorder or randomness in the system



Professor Stephen Hawking: Black hole



https://en.wikipedia.org/wiki/Chemical_reaction

<http://www.michelecoscia.com/?p=1041>

Note: The pictures taken from internet are only used to demonstrate the research idea. These pictures will not be used for publication or commercial purpose



the Fourth Law of Thermodynamics

- phenomenological equations:

A set of functions are used to express the linear dependence of these two flows on the corresponding forces.

$$\begin{aligned} J_1 &= L_{11}F_1 + L_{12}F_2 + \dots + L_{1k}F_k \\ J_2 &= L_{21}F_1 + L_{22}F_2 + \dots + L_{2k}F_k \\ J_k &= L_{k1}F_1 + L_{k2}F_2 + \dots + L_{kk}F_k \\ J_i &= \sum_{k=1}^n L_{jk} F_k \quad (j = 1, 2, 3, \dots, n) \end{aligned}$$



Lars Onsager
Nobel Prize in Chemistry in 1968



Contents

1. Introduction

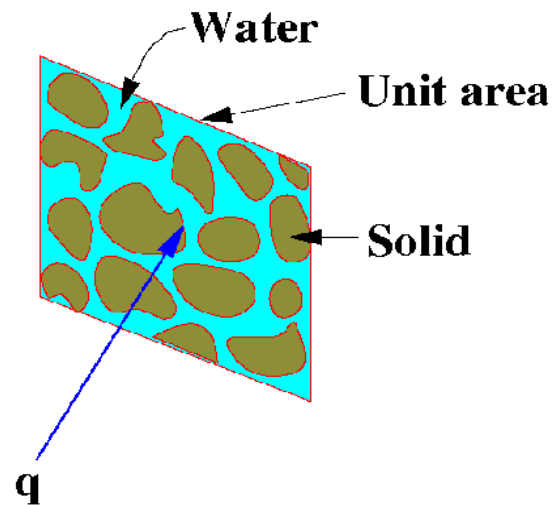
2. Methodology

3. New Matrix

4. Modelling

5. End

Solid and fluid



Dissipation generated by frictional resistance at solid and fluid interface

$$0 \leq T\gamma = -\mathbf{I}^w \cdot \nabla \mu^w - \mathbf{I}^c \cdot \nabla \mu^c$$

Gibbs-duhem equation

$$0 \leq T\gamma = -\mathbf{u} \cdot \nabla p - (\mathbf{J}^w \cdot \nabla \mu^w + \mathbf{J}^c \cdot \nabla \mu^c)$$

Note: Since the diffusion fluxes of the water and chemical relative to the barycentric motion can be written as

$$\mathbf{J}_\beta = \tilde{\rho}_\beta (\mathbf{v}_\beta - \mathbf{v}_f)$$



Extending of Fick's diffusion law and Darcy's laws

$$\mathbf{u} = -k \frac{k_{rw}}{\theta} (\nabla p - r \frac{\rho_t^f}{C^w} \frac{\partial \mu^c}{\partial C^c} \nabla C^c)$$

$$\mathbf{J}^c = L \rho_t^f \frac{\nabla p}{p} - \rho_t^f D \nabla C^c$$

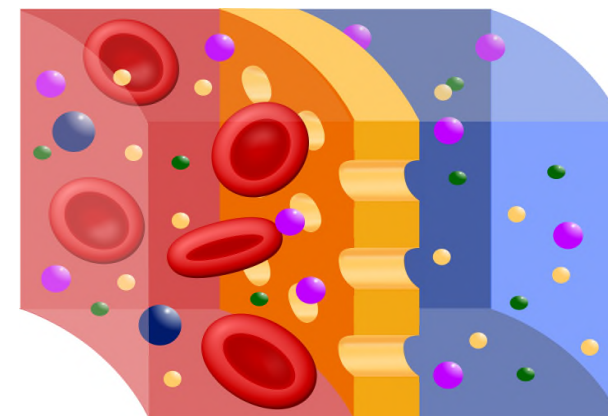
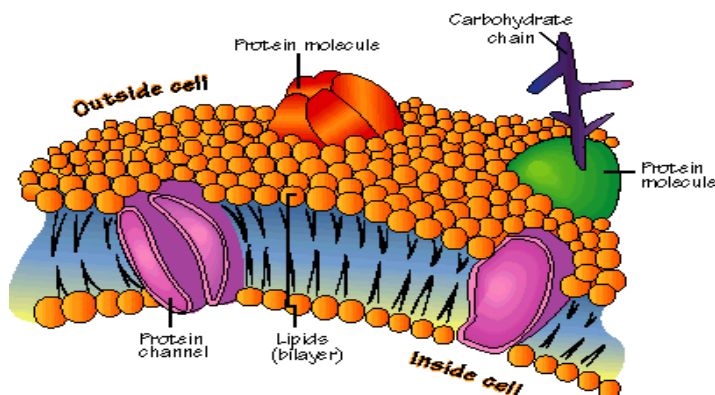
where

$$k \frac{k_{rw}}{\theta} = \frac{L^{11}}{(\rho_t^f)^2}$$

$$r = -\frac{L^{21}}{L^{11}}$$

$$L = \frac{L^{21} p}{(\rho_t^f)^2}$$

$$D = \frac{L^{22}}{C^w (\rho_t^f)^2} \frac{\partial \mu^c}{\partial C^c}$$



Darcy's Law and Fick's Law



UNIVERSITY OF LEEDS

$$\begin{pmatrix} \mathbf{u} \\ \mathbf{J}^s \end{pmatrix} = - \begin{bmatrix} \frac{k}{v} & \frac{kr_f \bar{\rho}_f}{v c_d} \frac{\partial \mu_s}{\partial c_s} \\ \frac{L \rho_f}{p} & \rho_f D \end{bmatrix} \begin{pmatrix} \text{grad } p \\ \text{grad } c_s \end{pmatrix}$$

$$\begin{pmatrix} \mathbf{u} \\ \mathbf{J}^s \end{pmatrix} = - \begin{bmatrix} \frac{k}{v} & 0 \\ 0 & \rho_f D \end{bmatrix} \begin{pmatrix} \text{grad } p \\ \text{grad } c_s \end{pmatrix}$$

CHEN, X., PAO, W., THORNTON, S. & SMALL, J. 2016. Unsaturated hydro-mechanical–chemical constitutive coupled model based on mixture coupling theory: Hydration swelling and chemical osmosis. *International Journal of Engineering Science* (IF:3.165), 104, 97-109.

Darcy's Law and Fourier's law of heat conduction



UNIVERSITY OF LEEDS

$$\begin{pmatrix} \mathbf{u} \\ \mathbf{q} \end{pmatrix} = - \begin{bmatrix} \frac{k}{v} & \frac{kr_q \bar{\rho}_f}{vT} \\ \frac{L_q \rho_f}{p} & \lambda \end{bmatrix} \begin{pmatrix} \text{grad } p \\ \text{grad } T \end{pmatrix}$$

$$\begin{pmatrix} \mathbf{u} \\ \mathbf{q} \end{pmatrix} = - \begin{bmatrix} \frac{k}{v} & 0 \\ 0 & \lambda \end{bmatrix} \begin{pmatrix} \text{grad } p \\ \text{grad } T \end{pmatrix}$$

CHEN, X., PAO, W. & LI, X. 2013. Coupled thermo-hydro-mechanical model with consideration of thermal-osmosis based on modified mixture theory. *International Journal of Engineering Science*, 64, 1-13.



Contents

1. Introduction

2. Methodology

3. New Matrix

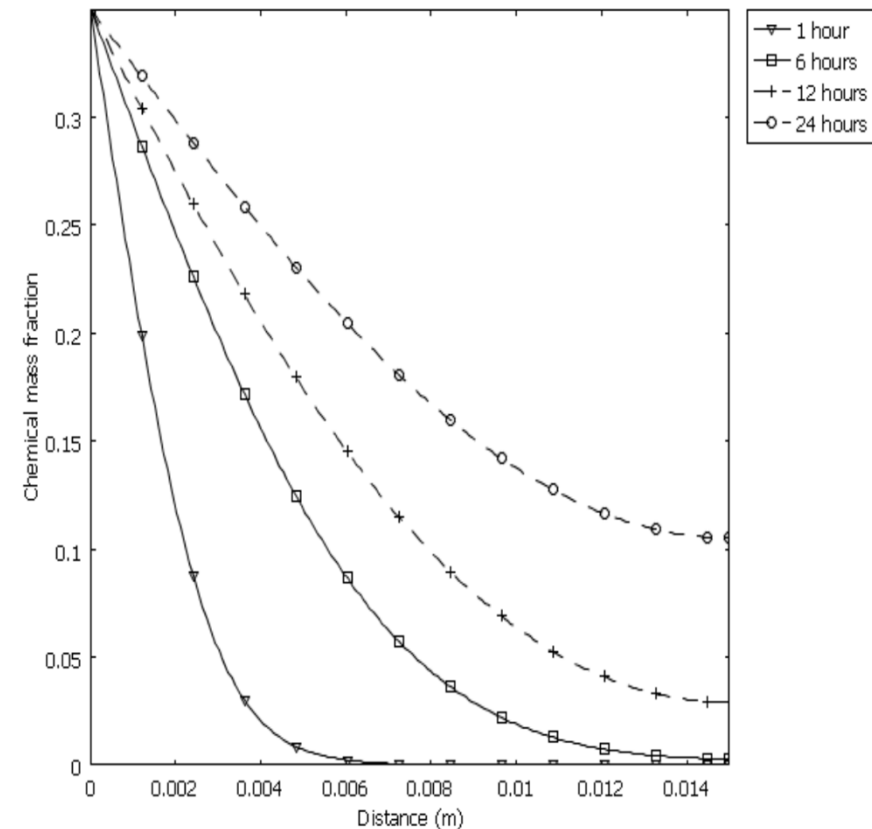
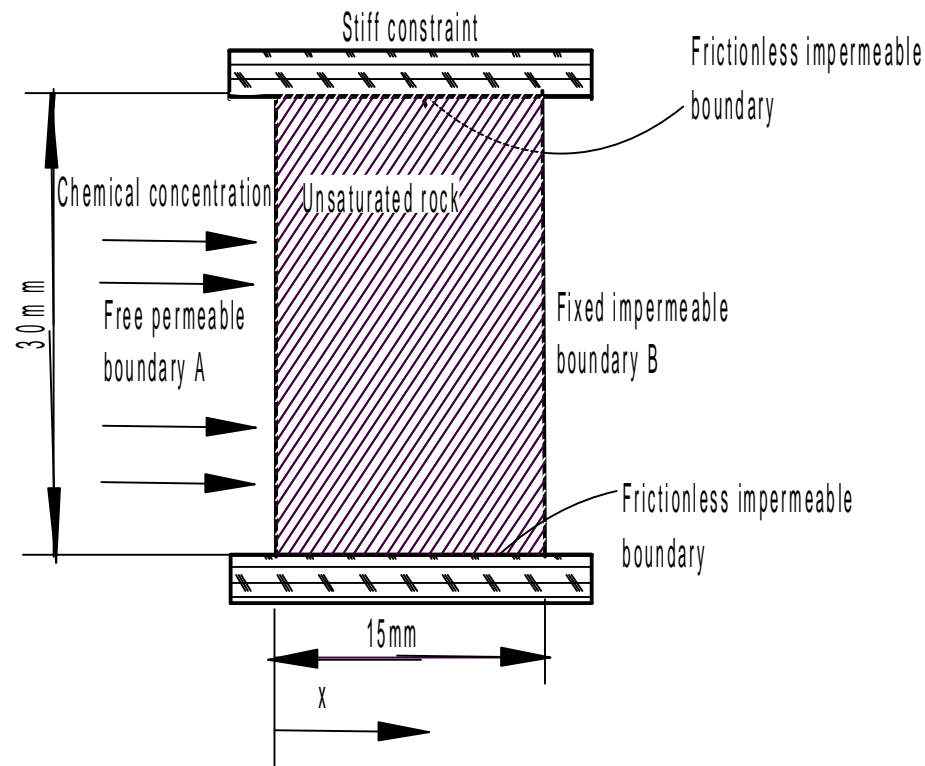
4. Modelling

5. End



(Experiment set up + chemical transport)

Invalidate Darcy's Law (1: Chemical osmosis)



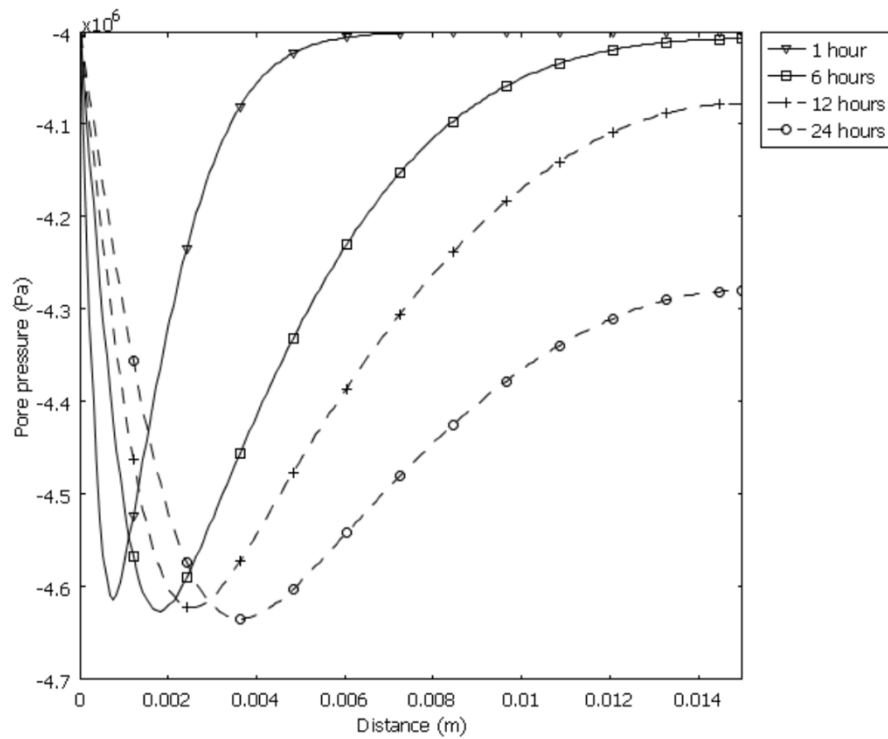


Fig. 3 Evolution of pore water pressure distribution with time during first day

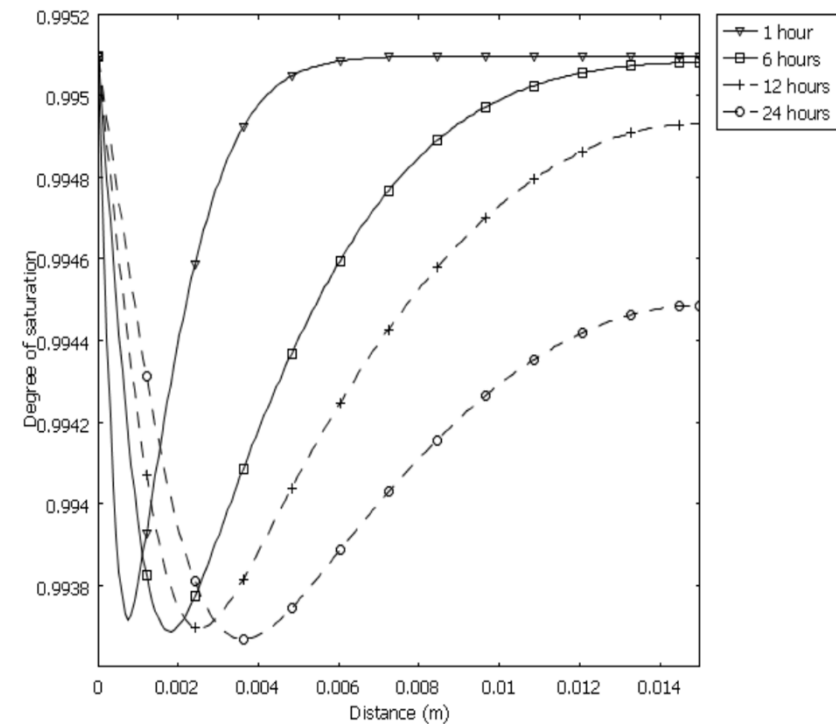


Fig. 4 Evolution of degree of saturation distribution with time during first day

Invalidate Darcy's Law (2: Thermo osmosis)

X. Chen et al./International Journal of Engineering Science 64 (2013) 1–13

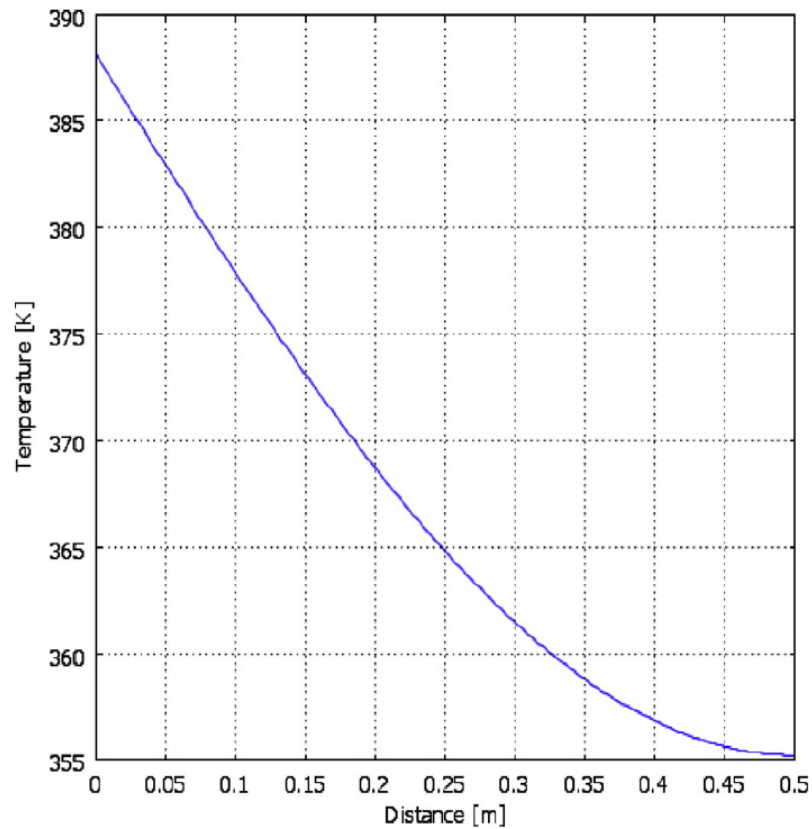
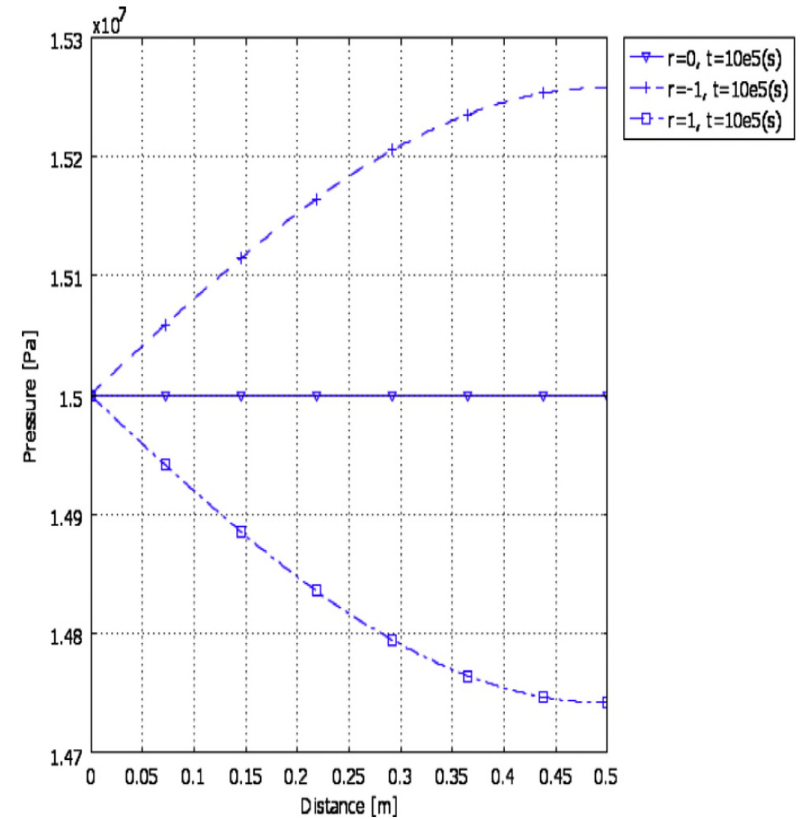


Fig. 5. Temperature distribution.





Contents

1. Introduction

2. Methodology

3. New Matrix

4. Modelling

5. End

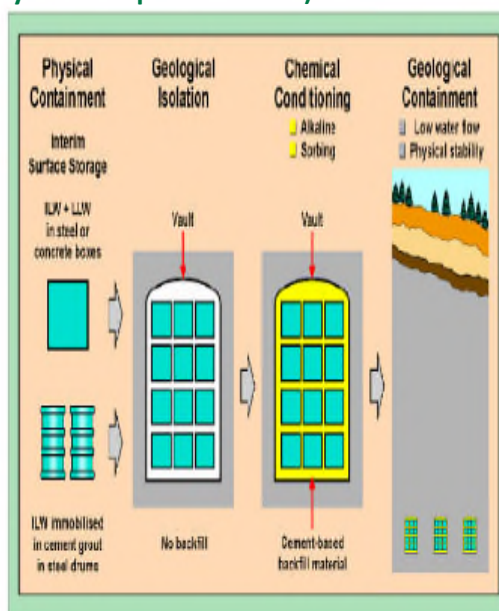


End, but not the End

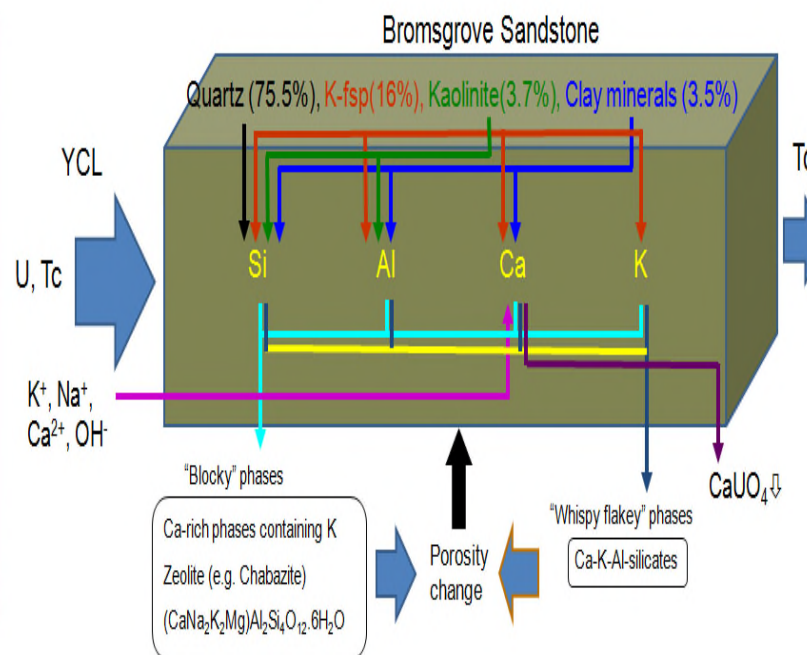
Intermediate/Low Level nuclear waste: Radionuclides transport through sandstone in groundwater

Darcy's Law, valid or not in a contaminant-impacted zone?

(Part 2: heavily reactive porous media)



Nuclear Waste Concept



(2) Conceptual model

Conclusion: multi-minerals dissolution strongly affects the pathway and chemistry of groundwater flow .

Corkhill, C; Bridge, J; **Chen, X**; Hillel, P; Thornton, S; Romero-Gonzalez, M; Banwart, S; Hyatt, N. (2013) Real-time gamma imaging of technetium transport through natural and engineered porous materials for radioactive waste disposal, *Environmental Science & Technology*, 47(23): 13857-1864.

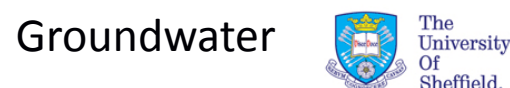
Chen, X., Thornton, S. F. & Small, J. Influence of Hyper-Alkaline pH Leachate on Mineral and Porosity Evolution in the Chemically Disturbed Zone Developed in the Near-Field Host Rock for a Nuclear Waste Repository. *Transport in Porous Media* 107, 489-505, doi:10.1007/s11242-014-0450-0 (2015).



UNIVERSITY OF LEEDS

Acknowledgement

New theory could boost engineering solutions/innovations...
... gap between theory and engineering application....



Available for consultancy;

Welcome industry partner to join our team to develop links with China industry and academy for applications to Innovate UK and Newton fund in the area of contaminated lands.

Contact information:

x.chen@leeds.ac.uk

Current funded project:

BioSAS consortium (around £580k)